

## Lucky Edge Labeling of $P_n$ , $C_n$ and Corona of $P_n$ , $C_n$

**Dr. A. Nellai Murugan**

Department of Mathematics,  
V.O.Chidambaram College,  
Tuticorin, Tamilnadu(INDIA)  
anellai.voc@gmail.com

**R. Maria Irudhaya Aspin Chitra**

Department of Mathematics,  
V.O.Chidambaram College,  
Tuticorin, Tamilnadu(INDIA)  
aspinvjs@gmail.com

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**Abstract:** Let  $G$  be a Simple Graph with Vertex set  $V(G)$  and Edge set  $E(G)$  respectively. Vertex set  $V(G)$  is labeled arbitrary by positive integers and let  $E(e)$  denote the edge label such that it is the sum of labels of vertices incident with edge  $e$ . The labeling is said to be lucky edge labeling if the edge set  $E(G)$  is a proper coloring of  $G$ , that is, if we have  $E(e_1) \neq E(e_2)$  whenever  $e_1$  and  $e_2$  are adjacent edges. The least integer  $k$  for which a graph  $G$  has a lucky edge labeling from the set  $\{1, 2, \dots, k\}$  is the lucky number of  $G$  denoted by  $\eta(G)$ .

A graph which admits lucky edge labeling is the lucky edge labeled graph. In this paper, it is proved that Path  $P_n$ , Comb  $P_n^+$ , Cycle  $C_n$ , Crown  $C_n^+$  are lucky edge labeled graphs.

**Keywords:** Lucky Edge Labeled Graph, Lucky Edge Labeling, Lucky Number, 2010 Mathematics subject classification Number: 05C78.

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### 1. INTRODUCTION

A graph  $G$  is a finite non empty set of objects called vertices together with a set of pairs of distinct vertices of  $G$  which is called edges. Each  $e = \{uv\}$  of vertices in  $E$  is called an edge or a line of  $G$ . For Graph Theoretical Terminology, [2].

### 2. PRELIMINARIES

#### Definition: 2.1

Let  $G$  be a Simple Graph with Vertex set  $V(G)$  and Edge set  $E(G)$  respectively. Vertex set  $V(G)$  are labeled arbitrary by positive integers and let  $E(e)$  denote the edge label such that it is the sum of labels of vertices incident with edge  $e$ . The labeling is said to be **lucky edge labeling** if the edge set  $E(G)$  is a proper coloring of  $G$ , that is, if we have  $E(e_1) \neq E(e_2)$  whenever  $e_1$  and  $e_2$  are adjacent edges. The least integer  $k$  for which a graph  $G$  has a lucky edge labeling from the set  $\{1, 2, \dots, k\}$  is the **lucky number** of  $G$  denoted by  $\eta(G)$ .

A graph which admits lucky edge labeling is the **lucky edge labeled graph**.

#### Definition: 2.2

A **Walk** of a graph  $G$  is an alternating sequence of vertices and edges  $v_1, e_1, v_2, e_2, \dots, v_{n-1}, e_n, v_n$  beginning and ending with vertices such that each edge  $e_i$  is incident with  $v_{i-1}$  and  $v_i$ .

#### Definition: 2.3

If all the vertices in a walk are distinct, then it is called a **Path** and a path of length  $n$  is denoted by  $P_{n+1}$ .

#### Definition: 2.4

A graph obtained by joining each  $u_i$  to a vertex  $v_i$  is called a **Comb** and denoted by  $P_n^+$ . The Vertex set and Edge set of  $P_n^+$  is  $V[P_n^+] = \{u_i, v_i: 1 \leq i \leq n\}$  and  $E[P_n^+] = \{(u_i, u_{i+1}): 1 \leq i \leq n-1\} \cup \{(u_i, v_i): 1 \leq i \leq n\}$  respectively.  $P_n^+$  has  $2n$  vertices and  $2n-1$  edges.

#### Definition: 2.5

A closed path is called a **Cycle** and a cycle of length  $n$  is denoted by  $C_n$ .

**Definition: 2.6**

$C_n^+$  is a graph obtained from  $G$  by attaching a pendent vertex from each vertex of the graph  $C_n$  is called **Crown**.

**3. MAIN RESULTS**

**Theorem: 3.1**

$P_n$  has  $\{a, b\}$  lucky edge labeling graph for any  $a, b \in N$ .

**Proof:**

Let  $V[P_n] = \{ u_i : 1 \leq i \leq n \}$  and  $E[P_n] = \{ (u_i, u_{i+1}) : 1 \leq i \leq n-1 \}$ .

Let  $f: V[P_n] \rightarrow \{1, 2\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}$$

and  $1 \leq i \leq (n-1)/2$ , for  $n$  is odd and  $1 \leq i \leq n/2$ , for  $n$  is even.

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}$$

and  $1 \leq i \leq (n+1)/2$ , for  $n$  is odd and  $1 \leq i \leq n/2$ , for  $n$  is even.

Then the induced edge coloring are

when  $n$  is odd,  $1 \leq i \leq (n-1)/2$  and when  $n$  is even,  $1 \leq i \leq (n/2) - 1$

$$f^*(u_{2i}u_{2i+1}) = 3$$

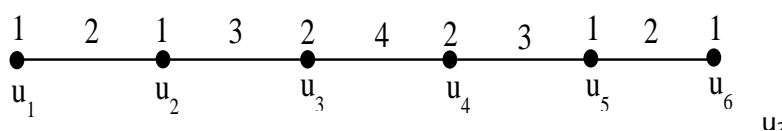
when  $n$  is odd,  $1 \leq i \leq (n-1)/2$  and when  $n$  is even,  $1 \leq i \leq n/2$

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}$$

It is clear that lucky edge labeling of  $P_n$  is  $\{2, 3, 4\}$ .

Hence,  $P_n$  has lucky edge labeling graph.

For example, lucky edge labeling of  $P_6$  is shown in figure 1 and  $\eta(P_n) = 4$ .



**Theorem: 3.2**

$P_n^+$  has  $\{a, b, c\}$  lucky edge labeling graph for any  $a, b, c \in N$ .

**Proof:**

Let  $V[P_n^+] = \{ \{u_i : 1 \leq i \leq n\}, \{v_i : 1 \leq i \leq n\} \}$  and  $E[P_n^+] = \{ (u_i, u_{i+1}) : 1 \leq i \leq n-1 \} \cup \{ (u_i, v_i) : 1 \leq i \leq n \}$ .

Let  $f: V[P_n^+] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}$$

and  $1 \leq i \leq (n-1)/2$ , for  $n$  is odd and  $1 \leq i \leq n/2$ , for  $n$  is even.

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}$$

and  $1 \leq i \leq (n+1)/2$ , for  $n$  is odd and  $1 \leq i \leq n/2$ , for  $n$  is even.

$$f(v_1) = 2$$

$$f(v_i) = 3, 2 \leq i \leq n-1$$

$$f(v_n) = \begin{cases} 1 & n \equiv 0, 1 \pmod{4} \\ 2 & n \equiv 2, 3 \pmod{4} \end{cases}$$

Then the induced edge coloring are

whenn is odd,  $1 \leq i \leq (n - 1)/2$  and when n is even,  $1 \leq i \leq (n/2) - 1$

$$f^*(u_{2i}u_{2i+1}) = 3$$

whenn is odd,  $1 \leq i \leq (n - 1)/2$  and when n is even,  $1 \leq i \leq n/2$

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}$$

$$f^*(u_1v_1) = 3$$

$$f^*(u_i v_i) = \begin{cases} 4 & i \equiv 1, 2 \pmod{4} \\ 5 & i \equiv 0, 3 \pmod{4} \end{cases} \text{ for } 2 \leq i \leq n-1.$$

$$f^*(u_n v_n) = \begin{cases} 3 & n \equiv 0 \pmod{2} \\ 2 & n \equiv 1 \pmod{4}. \\ 4 & n \equiv 3 \pmod{4} \end{cases}$$

It is clear that lucky edge labeling of  $P_n^+$  is  $\{2, 3, 4, 5\}$ .

Hence,  $P_n^+$  has lucky edge labeling graph.

For example, lucky edge labeling of  $P_5^+$  and  $P_6^+$  are given in the figure 2a and figure 2b and  $\eta(P_n^+) = 5$ .

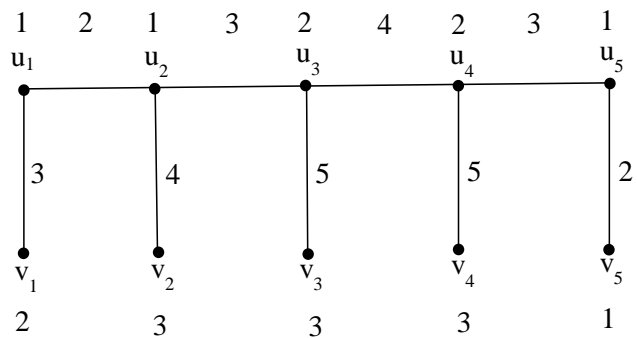


Figure 2a and  $\eta(P_n^+) = 5$

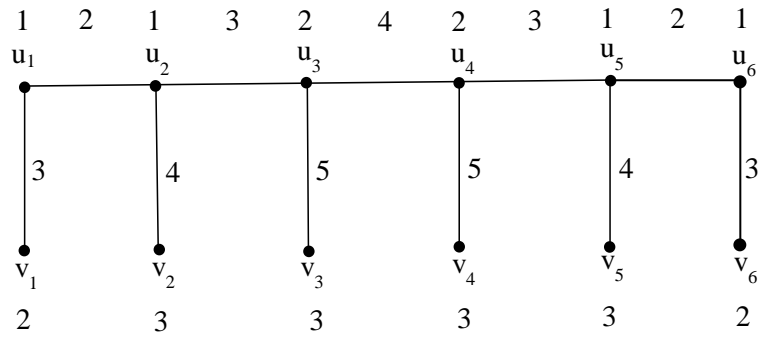


Figure 2b and  $\eta(P_n^+) = 5$

**Theorem 3.3:**

$C_n : n \equiv 1, 2, 3 \pmod{4}$  has  $\{a, b, c\}$  lucky edge labeling and

$C_n : n \equiv 0 \pmod{4}$  has  $\{a, b\}$  lucky edge labeling for any  $a, b, c \in N$ .

**Proof:**

Let  $V[C_n] = \{ u_i : 1 \leq i \leq n \}$  and  $E[C_n] = \{ \{ (u_i u_{i+1}) : 1 \leq i \leq n-1 \} \cup \{ (u_n u_1) \} \}$ .

Case 1:

Let  $C_n$  be the graph when  $n \equiv 0 \pmod{4}$ .

Let  $f: V[C_n] \rightarrow \{1, 2\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

Then the induced edge coloring are

when  $1 \leq i \leq (n/2) - 1$ ,

$$f^*(u_{2i}u_{2i+1}) = 3,$$

$$f^*(u_n u_1) = 3.$$

when  $1 \leq i \leq n/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

It is clear that the lucky edge labeling of  $C_n : n \equiv 0 \pmod{4}$  is  $\{2, 3, 4\}$ .

For example, Lucky edge labeling of  $C_4$  is given in the figure 3a and  $\eta(C_n) = 4$ .

Case 2:

Let  $C_n$  be the graph when  $n \equiv 1 \pmod{4}$ .

Let  $f: V[C_n] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_i) = 3, i \equiv 1 \pmod{4} \text{ and } i = n.$$

Then the induced edge coloring are

when  $1 \leq i \leq (n - 3)/2$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n - 1)/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

when  $i = n$ ,

$$f^*(u_i u_1) = 4 \text{ and } f^*(u_{i-1} u_i) = 5.$$

It is clear that the lucky edge labeling of  $C_n : n \equiv 1 \pmod{4}$  is clearly  $\{2, 3, 4, 5\}$ .

For example, Lucky edge labeling of  $C_5$  is shown in the figure 3b and  $\eta(C_n) = 5$ .

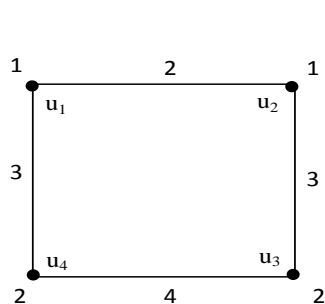


Figure 3a and  $\eta(C_n) = 4$

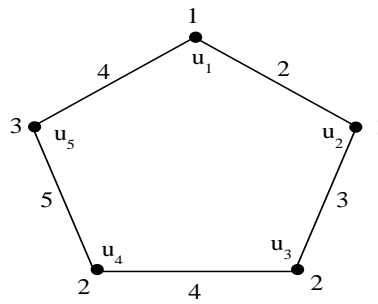


Figure 3b and  $\eta(C_n) = 5$

Case 3:

Let  $C_n$  be the graph when  $n \equiv 2 \pmod{4}$ .

Let  $f: V[C_n] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n/2) - 1.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n/2) - 1.$$

$$f(u_i) = 3, \begin{cases} i \equiv 1 \pmod{4} \\ i \equiv 2 \pmod{4} \end{cases} \text{ and } i = n, n-1.$$

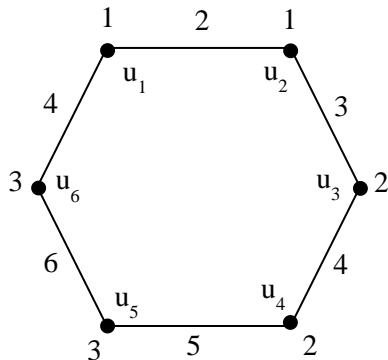


Figure 3c and  $\eta(C_n) = 6$

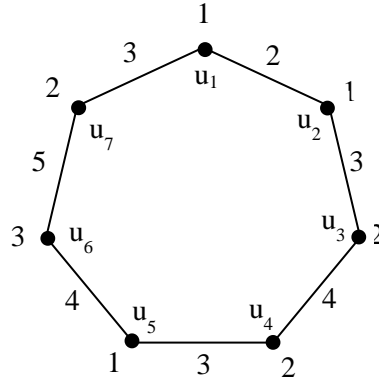


Figure 3d and  $\eta(C_n) = 5$

Then the induced edge coloring are

when  $1 \leq i \leq (n/2) - 2$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n/2) - 1$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

when  $i = n-1$  and  $n-2$ ,

$$f^*(u_i u_{i+1}) = \begin{cases} 5 & i \equiv 0 \pmod{4} \\ 6 & i \equiv 1 \pmod{4} \end{cases}.$$

$$f^*(u_n u_1) = 4.$$

It is clear that the lucky edge labeling of  $C_n : n \equiv 2 \pmod{4}$  is clearly  $\{2, 3, 4, 5, 6\}$ .

For example, Lucky edge labeling of  $C_6$  is shown in the figure 3c and  $\eta(C_n) = 6$ .

Case 4:

Let  $C_n$  be the graph when  $n \equiv 3 \pmod{4}$ .

Let  $f: V[C_n] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n-3)/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n+1)/2 \text{ and } i = n-1$$

$$f(u_i) = 3, i \equiv 2 \pmod{4}.$$

Then the induced edge coloring is

when  $1 \leq i \leq (n-3)/2$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n-3)/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

$$f^*(u_{i-1}u_i) = \begin{cases} 4 & \text{when } i = n-1 \\ 5 & \text{when } i = 1 \end{cases} \text{ and } f^*(u_n u_1) = 3.$$

It is clear that the lucky edge labeling of  $C_n : n \equiv 3 \pmod{4}$  is clearly  $\{2, 3, 4, 5\}$ . For example, Lucky edge labeling of  $C_7$  is shown in the figure 3d and  $\eta(C_n) = 5$ . Hence,  $C_n$  has lucky edge labeling graph.

**Theorem 3.4:**

$C_n^+ : n \equiv 0, 1, 2, 3 \pmod{4}$  has  $\{a, b, c\}$  lucky edge labeling for any  $a, b, c \in \mathbb{N}$ .

**Proof:**

Let  $V[C_n^+] = \{u_i : 1 \leq i \leq n\}$  and  $\{v_i : 1 \leq i \leq n\}$  and

$E[C_n^+] = \{(u_i u_{i+1}) : 1 \leq i \leq n-1\} \cup \{(u_n u_1)\} \cup \{(u_i v_i) : 1 \leq i \leq n\}$ .

Case 1:

Let  $C_n^+$  be the graph when  $n \equiv 0 \pmod{4}$ .

Let  $f: V[C_n] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(v_i) = 3, 1 \leq i \leq n.$$

Then the induced edge coloring are

when  $1 \leq i \leq (n/2) - 1$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

$$f^*(u_n u_1) = 3.$$

when  $1 \leq i \leq n/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

when  $1 \leq i \leq n$ ,

$$f^*(u_i v_i) = \begin{cases} 4 & i \equiv 1, 2 \pmod{4} \\ 5 & i \equiv 0, 3 \pmod{4} \end{cases}.$$

It is clear that the lucky edge labeling of  $C_n^+ : n \equiv 0 \pmod{4}$  is  $\{2, 3, 4, 5\}$ .

For example, Lucky edge labeling of  $C_4^+$  is shown in the figure 4a and  $\eta(C_n^+) = 5$ .

Case 2:

Let  $C_n^+$  be the graph when  $n \equiv 1 \pmod{4}$ .

Let  $f: V[C_n^+] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq n/2.$$

$$f(u_i) = 3, i \equiv 1 \pmod{4} \text{ and } i = n.$$

$$f(v_1) = 2, f(v_{n-1}) = 1$$

$$f(v_i) = 3, 2 \leq i \leq n.$$

Then the induced edge coloring are

when  $1 \leq i \leq (n - 3)/2$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n - 1)/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}.$$

when  $i = n$ ,

$$f^*(u_i u_1) = 4 \text{ and } f^*(u_{i-1} u_i) = 5.$$

when  $n-2 \leq i \leq n$ ,

$$f^*(u_i v_i) = \begin{cases} 5 & i \equiv 3 \pmod{4} \\ 3 & i \equiv 0 \pmod{4} \\ 6 & i \equiv 1 \pmod{4} \end{cases}$$

$$f^*(u_1 v_1) = 3.$$

when  $2 \leq i \leq n-3$ ,

$$f^*(u_i v_i) = \begin{cases} 4 & i \equiv 1, 2 \pmod{4} \\ 5 & i \equiv 0, 3 \pmod{4} \end{cases}$$

It is clear that the lucky edge labeling of  $C_n^+ : n \equiv 1 \pmod{4}$  is  $\{2, 3, 4, 5, 6\}$ .

For example, Lucky edge labeling of  $C_5^+$  is shown in the figure 4b and  $\eta(C_n^+) = 6$ .

Case 3:

Let  $C_n^+$  be the graph when  $n \equiv 2 \pmod{4}$ .

Let  $f: V[C_n^+] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n/2) - 1.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n/2) - 1.$$

$$f(u_i) = 3, \begin{matrix} i \equiv 1 \pmod{4} \\ i \equiv 2 \pmod{4} \end{matrix} \text{ and } i = n, n-1.$$

$$f(v_1) = 1, i = n-1, n-2 \text{ and } f(v_i) = 2, i = 1, n.$$

$f(v_i) = 3, 2 \leq i \leq n-3$ .

Then the induced edge coloring are

when  $1 \leq i \leq (n/2) - 2$ ,

$$f^*(u_{2i} u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n/2) - 1$ ,

$$f^*(u_{2i-1} u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}$$

when  $i = n-1, n-2$ ,

$$f^*(u_i u_{i+1}) = \begin{cases} 5 & i \equiv 0 \pmod{4} \\ 6 & i \equiv 1 \pmod{4} \end{cases}$$

$$f^*(u_n u_1) = 4.$$

when  $i = 1, n-2$ ,

$$f^*(u_i v_i) = 3.$$

when  $2 \leq i \leq n-1$ ,

$$f^*(u_i v_i) = \begin{cases} 4 & i \equiv 1, 2 \pmod{4} \\ 5 & i \equiv 0, 3 \pmod{4} \end{cases}$$

$$f^*(u_i v_i) = 5, i = n.$$

It is clear that the lucky edge labeling of  $C_n^+ : n \equiv 2 \pmod{4}$  is  $\{2, 3, 4, 5, 6\}$ .

For example, Lucky edge labeling of  $C_6^+$  is shown in the figure 4c and  $\eta(C_n^+) = 6$ .

Case 4:

Let  $C_n^+$  be the graph when  $n \equiv 3 \pmod{4}$ .

Let  $f: V[C_n^+] \rightarrow \{1, 2, 3\}$  defined by

$$f(u_{2i}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n-3)/2.$$

$$f(u_{2i-1}) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 2 & i \equiv 0 \pmod{2} \end{cases}, 1 \leq i \leq (n+1)/2 \text{ and } i = n-1$$

$$f(u_i) = 3, i \equiv 2 \pmod{4}.$$

$$f(v_i) = \begin{cases} 2 & i \equiv 3 \pmod{4} \\ 3 & i \equiv 2 \pmod{4}, n-2 \leq i \leq n. \\ 1 & i \equiv 1 \pmod{4} \end{cases}$$

$$f(v_i) = 3, 1 \leq i \leq n-3.$$

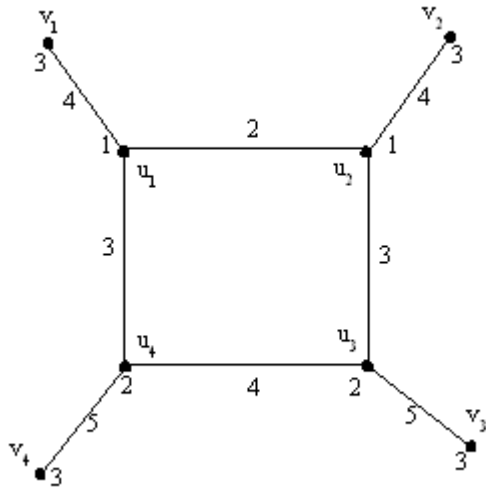


Figure 4a and  $\eta(C_n^+) = 5$

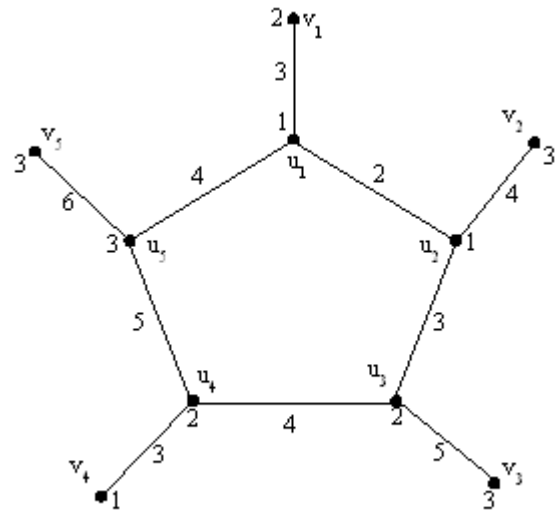


Figure 4b and  $\eta(C_n^+) = 6$

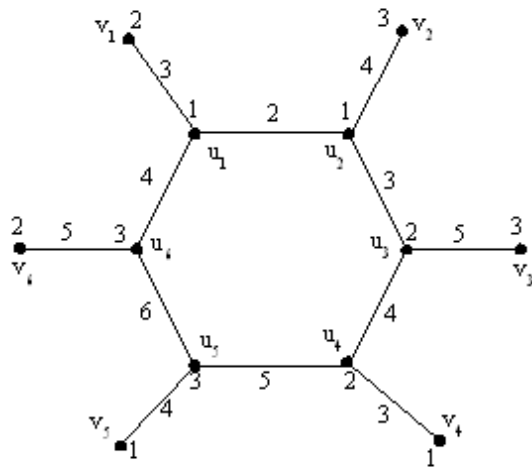


Figure 4c and  $\eta(C_n^+) = 6$

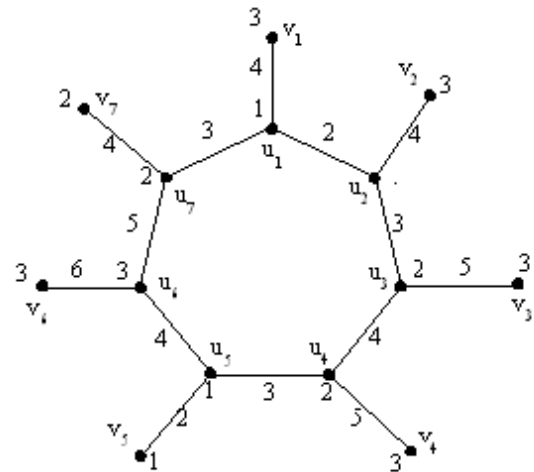


Figure 4d and  $\eta(C_n^+) = 6$

Then the induced edge coloring are

when  $1 \leq i \leq (n-3)/2$ ,

$$f^*(u_{2i}u_{2i+1}) = 3.$$

when  $1 \leq i \leq (n-3)/2$ ,

$$f^*(u_{2i-1}u_{2i}) = \begin{cases} 2 & i \equiv 1 \pmod{2} \\ 4 & i \equiv 0 \pmod{2} \end{cases}$$

$$f^*(u_{i-1}u_i) = \begin{cases} 4 & \text{when } i = n-1 \\ 5 & \text{when } i = 1 \end{cases}$$

$$f^*(u_n u_1) = 3.$$

when  $n-2 \leq i \leq n$ ,

$$f^*(u_i v_i) = \begin{cases} 2 & i \equiv 1 \pmod{3} \\ 6 & i \equiv 2 \pmod{3} \\ 4 & i \equiv 0 \pmod{3} \end{cases}$$

when  $1 \leq i \leq n-3$ ,

$$f^*(u_i v_i) = \begin{cases} 4 & i \equiv 1, 2 \pmod{4} \\ 5 & i \equiv 0, 3 \pmod{4} \end{cases}$$



It is clear that the lucky edge labeling of  $C_n^+ : n \equiv 3 \pmod{4}$  is  $\{2, 3, 4, 5, 6\}$ .

For example, Lucky edge labeling of  $C_7^+$  is shown in the figure 4d and  $\eta(C_n^+) = 6$ .

Hence,  $C_n^+$  has lucky edge labeling graph.

#### **4. CONCLUSION**

Among all labelling lucky edge labelling has a special importance because it is incorporated with coloring of graphs

#### **REFERENCES**

- [1] GALLIAN.J.A, *A Dynamical survey of graphs Labeling*, The Electronic Journal of combinatorics. 6(2001) #DS6.
- [2] HARRARY.F, *Graph Theory*, Adadison-Wesley Publishing Company Inc, USA, 1969.
- [3] NELLAIMURUGAN.A- *STUDIES IN GRAPH THEORY –SOME LABELING PROBLEMS IN GRAPHS AND RELATED TOPICS*, Ph.D, Thesis September 2011...

#### **AUTHORS' BIOGRAPHY**



**Dr. A. Nellai Murugan** is working as a Associate Professor in the Department of Mathematics, V.O. Chidambaram College, Tuticorin. He has 30 years of teaching experience and 10 years of research experience. He has participated in number of conferences/seminar at national and international level. He has published more than 40 research article in the reputed research journals. He is guiding 6 Ph.D research scholars.



**R. Maria Irudhaya Aspin Chitra** is a full time Ph.D Research Scholar working in Graph theory at Department of Mathematics, V.O. Chidambaram College, Tuticorin. She has communicated 3 more research articles