



Validity of the Criterion $pK_a = pH$ at the Half Equivalence Point for the Potentiometric Evaluation of the Ionization Constant of a Monoprotic Acid

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Abstract: The aim of this paper is to draw attention to the conditions under which the potentiometric evaluation of the acidity constant of a monoprotic acid, HA, can be performed from the single half point titration curve. We may usually adopt the pH corresponding to this point, $pH_{T=0.5}$, as the pK_a value avoiding the need of using a rigorous method of calculation involving the entire V-pH titration data. The complete and approximate theoretical relationships that allow making effective that choice have been derived. A literature search have been carried out in order to gather a number of papers in which the criterion $pK_a = pH_{0.5}$ has been used. In spite of the frequency with which this criterion is applied, it is only valid in favourable cases. A number of practical cases are included for study.

Keywords: Ionization constant; Half equivalence point; Potentiometric Measurements; Monoprotic acid

1. INTRODUCTION

The location of inflection points in S-shaped titration curves is a recurrent topic in analytical chemistry, and some recent papers [1, 2] have been published on this respect. The basic papers concerning the location of inflexion points of weak acid-strong basic titrations date [3-5] from the 1960's. Meites et al. [3, 4] include the dilution in their treatment thus arriving at conclusions different from those previously stated by Roller [6-8]. The equivalence versus inflexion points has been the subject of a paper from Stokes [9]. On the other hand Fournaise and Petitfaux [10] have also studied the limits to the use of inflection points as points of equivalence in the treatment of acid-base titration data.

A number of papers (Table 1) adopt as criterion for the calculation of acidity constants that the pK_a value coincides with the pH corresponding to the half point titration, $T(\text{fraction titrated})=0.5$, the ionic strength being fixed. This practice is extended, but some limitations on its use are apparent. An approximation to this topic is made in this paper following the Meites et al guidelines [3, 4] with the purpose of bringing some light to the subject but fleeing from complex mathematical treatments. Some practical cases have been tackled.

Table 1. Selected papers in which the criterion $pK_a = pH_{T=1/2}$ (half titration) is applied

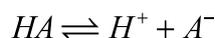
Comment	Ref.
Study of the X-ray structure of an anion complexed by a HBD receptor at the half-equivalence point.	[13]
Study of the deprotonation at the half-equivalence point of (thio)amido-benzimidazoles in the presence of anions.	[14]
Book including 35 advanced chemistry experiments designed for use with Vernier data-collection technology.	[15]
Evaluation of thiol Raman activities and pK_a values using internally referenced raman-based pH titration.	[16]
Investigation to identify and assess the factors causing systematic errors in the degree of deacetylation obtained from pH-potentiometric titrations.	[17]
A challenge to the readers in order to prove that the iconic $pK_a = pH_{1/2}$ is just a simplification of a more complex equation	[18]

A demonstration of why the simple equation $pH_{1/2} = pK_a$ still survives in all analytical chemistry textbooks despite its poor predicting power.	[19]
Method involving $EP_{1/2}$ is further investigated in order to obtain more accurate and precise results.	[20]
A method for the determination of acidity constants by feedback-based flow ratiometry and half equivalence point ($EP_{1/2}$) estimation.	[21]
High-performance liquid chromatography as a technique to determine pK_a values of drug candidates that show poor solubility in water.	[22]
Determination of dissociation constants of weak acids by feedback-based flow ratiometry.	[23]
Study of the micro-volume flow titration and screening the dissociation constants (pK_a) of weak acids.	[24]
Description of a simple method for calculating acidity parameters, as well as constants for the modified Henderson–Hasselbach equation.	[25]
Teaching students how to make a qualitative sketch of the expected titration curve helps to focus attention on the general principles.	[26]
Overview on theoretical works on potentiometric titration of ion exchangers.	[27]
Letter to editor about a simpler approach to “apparent” pK_a s based on a recent paper published by Cawley, 1995.	[28]
Titration and determination of "apparent" pK_a s. It challenges the students to do some critical about of the technique using pH at one-half titration over the whole pH scale.	[29]
Titration and determination of "apparent" pK_a s of very weak acids with some critical about using pH at one-half titration over the whole pH scale.	[30]
Potentiometric study of methanoic acid and glucuronic acid using a well-established experimental technique for suspensions of cellulosic fibers.	[31]
A laboratory experiment for the determination of pK_a using the half-volume method.	[32]
Calculation of the end point position of the potentiometric titration curve for boric acid.	[5]
Evaluation of the locations of points at which $pH = pK_a$ on potentiometric acid-base titration curve.	[4]
Investigation of the locations of inflection points on acid-base and related titration curves.	[3]
Potentiometric titration of weak acids and bases in dilute aqueous solution.	[33]

1.1. Theory

Basic Relationships

The equilibrium of acid dissociation of a weak monoprotic acid is given by



being the corresponding mixed (apparent) acidity constant at an ionic strength (I) fixed

$$K_a = \frac{(H^+)[A^-]}{[HA]} \quad (1)$$

where parenthesis indicate activities and brackets concentrations. In titrating an initial volume V_0 of a solution of HA of concentration C_A with a volume of a solution of strong monoprotic base, BOH, of concentration C_B we have

$$C_A \frac{V_0}{V_0 + V} = [HA] + [A^-] \quad (2)$$

$$[A^-] + [OH^-] = [B^+] + [H^+] = C_B \frac{V}{V_0 + V} + [H^+] \quad (3)$$

for the mass balance and the electroneutrality rule, respectively. Then

$$[A^-] = C_B \frac{V}{V_0 + V} + \Delta \quad (4)$$

where

$$\Delta = [H^+] - [OH^-] = \frac{(H^+)}{\gamma_{H^+}} - \frac{(OH^-)}{\gamma_{OH^-}} = \frac{(H^+)}{\gamma_{H^+}} - \frac{K_w^T}{(H^+)\gamma_{OH^-}} \quad (5)$$

where γ_H and γ_{OH} are the activity factors of hydrogen and hydroxide ion, respectively, which may be evaluated [11] from Debye and Hückel.

By combining Eqns. (1), (2) and (4) we get

$$K_a = (H^+) \frac{T + \frac{\Delta}{C_A \frac{V_0}{V_0+V}}}{1 - T - \frac{\Delta}{C_A \frac{V_0}{V_0+V}}} \quad (6)$$

where T is the titrated fraction

$$T = \frac{C_B V}{C_A V_0} \quad (7)$$

In those cases in which the second term of the numerator of the right hand of Eqn. (6) can be despised against T and (1-T), we obtain

$$K_a \approx (H^+) \frac{T}{1-T} \quad (8)$$

and then at the half titration, when $T=0.5$ we get

$$pK_a \approx pH_{T=0.5} \quad (9)$$

Note that [12]

$$\tilde{n} = \frac{C_H - [H^+]}{C_A \frac{V_0}{V_0+V}} = \frac{[HA]}{C_A \frac{V_0}{V_0+V}} = f = 1 - T - \frac{\Delta}{C_A \frac{V_0}{V_0+V}} \quad (10)$$

and then

$$K_a = (H^+) \frac{1 - \tilde{n}}{\tilde{n}} \quad (11)$$

and thus it is always true that

$$pK_a = pH_{\tilde{n}=0.5} \quad (12)$$

Derivation of the Relationship Between the Titrated Fraction When $pH=pK_a$ as a Function of the Concentration and the Acidity Constant

From Eqn. (6) by simple algebra we get

$$-[H^+]^3 - \left(K_a + T C_A \frac{V_0}{V_0+V} \right) [H^+]^2 + \left((1-T) C_A K_a \frac{V_0}{V_0+V} + K_w \right) [H^+] + K_a K_w = 0 \quad (13)$$

and taking into account that

$$y = \frac{[H^+]}{K_a} \quad (14)$$

$$r = \frac{C_A}{C_B} \quad (15)$$

$$\frac{V_0}{V_0 + V} = \frac{1}{1 + \frac{V}{V_0}} = \frac{1}{1 + T \frac{C_A}{C_B}} = \frac{1}{1 + T r} \quad (16)$$

we get

$$y^3 + \left(1 + \frac{C_A}{K_a} \left(\frac{T}{1 + rT}\right)\right) y^2 - \left(\left(\frac{1 - T}{1 + rT}\right) \frac{C_A}{K_a} + \frac{K_w}{K_a^2}\right) y - \frac{K_w}{K_a^2} = 0 \quad (17)$$

From Eqn. (14), $y=1$, when

$$pH_{y=1} = pK_a \quad (18)$$

making thus possible to evaluate the value of T at this point

$$2 + \frac{C_A}{K_a(1 + r T_{y=1})} (2 T_{y=1} - 1) - 2 \frac{K_w}{K_a^2} = 0 \quad (19)$$

which on rearrangement gives

$$T_{y=1} = \frac{0.5 + \frac{K_a}{C_A} \left(\frac{K_w}{K_a^2} - 1\right)}{1 + r \frac{K_a}{C_A} \left(1 - \frac{K_w}{K_a^2}\right)} \quad (20)$$

Thus, the variation of the value of T when the $pH = pK_a$ ($y=1$) as a function of the concentration ($pC_A = -\log C_A$), at different pK_a values between 3 and 11 is shown in Fig. 1, for values of $r = C_A / C_B = 1$. The variation of the value of T (for $y=1$) as a function of concentration, for values of $pK_a = 9, 10.2$ and 3.5 , and different values of r (1, 0.1, 0.05 and 0) is shown in Fig. 2. In Fig. 3 the variation of the values of T (when $y=1$) as a function of pC_A is observed for pK_a values between 5.0 and 4.0. Finally, Fig. 4 shows the variation of the values of T ($pH = pK_a$) as a function of pK_a for pC_A values between 1.0 and 5.0. A look at the figures reveals that the mistake made taken T as 0.5 is null when the $pK_a = pK_w/2$ and increases as the pK_a distances from $pK_w/2$ and decreases the concentration C_A and increases the ratio $r = C_A / C_B$.

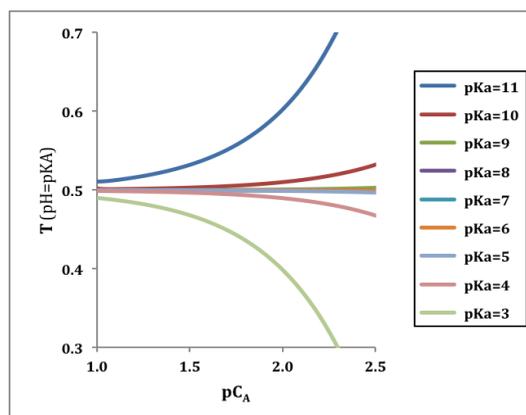


Figure1. Variation of the value of T when the $pH = pK_a$ ($y=1$) as a function of the concentration ($pC_A = -\log C_A$), at different pK_a values.

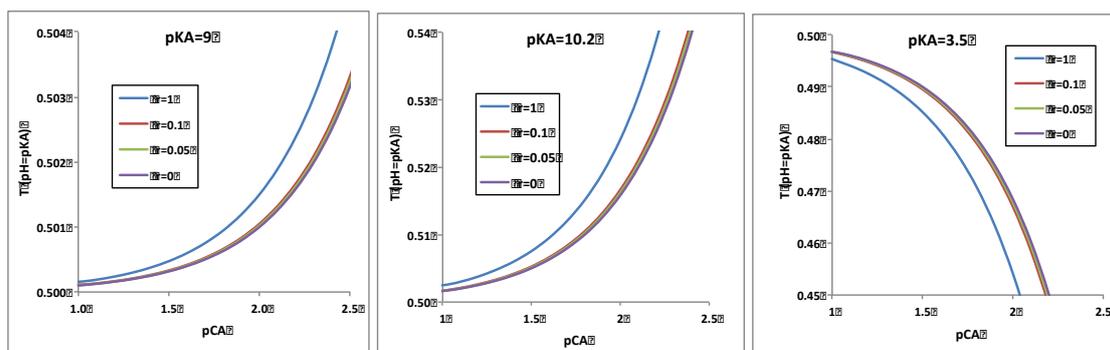


Figure2. Variation of the value of T (for $y=1$) as a function of concentration and different values of r ; $pK_a = 9$ (left), 10.2 (middle) and 3.5 (right).

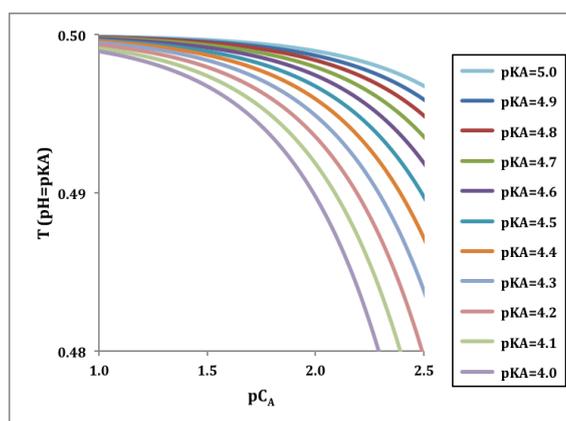


Figure3. Variation of the values of T (when $y=1$) as a function of pC_A ; pK_a values between 5.0 and 4.0

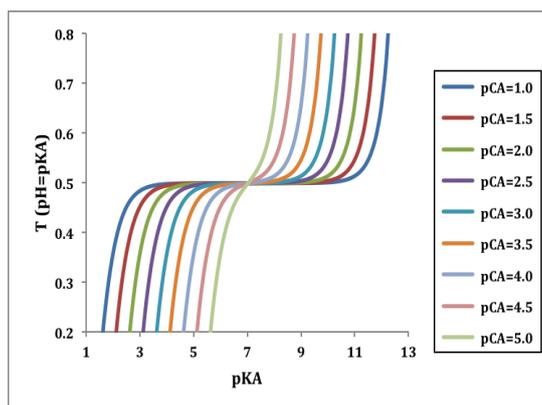


Figure4. Variation of the values of T ($pH = pK_a$) as a function of pK_a for pC_A values between 1.0 and 5.0 .

Bilogarithmic Method for the Evaluation of the Acidity Constants

From Eqn. (11) we have

$$\log \left(\frac{\tilde{n}}{1-\tilde{n}} \right) = pK_a - pH \quad (21)$$

where the value of \tilde{n} may be calculated at any point of titration by applying Eqn. (10).

Plotting the left hand of Eqn. (21) against pH a straight line ($y = a_0 + a_1 x$) of slope minus unity and intercept equal to pK_a is obtained, from [34, 35] the least squares method. The pK_a value is obtained at the point which cut the abscissa (pH) axis (because the experimental slope differs from the theoretical slope of minus unity), and then

$$pK_a = - \frac{a_0}{a_1} \quad (22)$$

Error Analysis

Note from Eqn. (22) that

$$pK_a = f(a_0, a_1) \quad (23)$$

and then by applying the random error propagation law [36, 37]

$$s_{pK_a}^2 = \left(\frac{\partial pK_a}{\partial a_0} \right) s_0^2 + \left(\frac{\partial pK_a}{\partial a_1} \right) s_1^2 + 2 \left(\frac{\partial pK_a}{\partial a_0} \right) \left(\frac{\partial pK_a}{\partial a_1} \right) \text{cov}(a_0, a_1) \quad (24)$$

and then taking into account Eqns. (22) and (24) by simple algebra we obtain

$$s_{pK_a} = \sqrt{\frac{1}{a_0^2} s_0^2 + \frac{a_0^2}{a_1^4} s_1^2 - 2 \frac{a_0}{a_1^3} \text{cov}(a_0, a_1)} \quad (25)$$

The Excel function LINNTEST [38] gives the parameters of the straight line (a_0 and a_1) and their corresponding standard deviations, and the standard deviation of the regression line, $s_{y/x}$. The covariance function may then easily estimated from

$$\text{cov}(a_0, a_1) = -\bar{x} \frac{s_{y/x}^2}{S_{xx}} = -\bar{x} s_a^2 \quad (26)$$

Mixed (Apparent) Acidity Constant and Thermodynamic Acidity Constant

The relationships between the thermodynamic pK_a^T and the mixed or apparent pK_a is given by

$$K_a^T = \frac{(H^+)(A^-)}{(HA)} = K_a \frac{\gamma_0}{\gamma_1} \quad (27)$$

$$pK_a^T = pK_a - \log \frac{\gamma_0}{\gamma_1} = pK_a - \log \gamma_0 \quad (28)$$

where γ_0 and γ_1 are the activity factors of the species A and HA, respectively $(H_jA) = \gamma_j [HA]$; the value of the γ_1 of the neutral species is assumed to be the unity.

Working at varying ionic strength we get

$$\log \left(\frac{\tilde{n}}{1-\tilde{n}} \right) - \log \gamma_0 = pK_a^T - pH \quad (29)$$

Note that in those cases in which Eqn. (10) may be simplified to give $\tilde{n}=1-T$ then at the half titration ($T=0.5$) follows

$$pK_a \approx pK_a^T + \log \gamma_{0(T=0.5)} \approx pH_{T=0.5} \quad (30)$$

The activity coefficient of an ion of z charge is given by

$$-\log \gamma_i = \frac{Az^2 \sqrt{I}}{1 + B a_i \sqrt{I}} \quad (31)$$

where A and B are constants [11] depending of the dielectric constant and temperature of solvent and a_i is the average distance of approximation of ions

The activity factor is depending of the ionic strength of the medium

$$I = \frac{1}{2} \sum C_i z_i^2 = \frac{1}{2} ([B^+] + [H^+] + [A^-] + [OH^-]) \quad (32)$$

where C_i are the concentration of the ions involved and z_i its charge. By combining Eqns. (3) and (32) we get

$$I = [B^+] + [H^+] = \frac{C_B V}{V_0 + V} + \frac{(H^+)}{\gamma_{H^+}} \quad (33)$$

Note that for either a cationic acid of the type HA^+ (i.e. ammonium ion, NH_4^+) or a neutral monoacid base B (i.e. TRIS which on protonation gives the species HB^+), the relationship between the thermodynamic and apparent constant is given by

$$pK_a^T = pK_a + \log \gamma_1 \quad (34)$$

being now γ_1 the activity coefficient of the species positively charged (i.e. HA^+). The expression applicable now for the potentiometric evaluation of the acidity constants is

$$\log \left(\frac{\tilde{n}}{1 - \tilde{n}} \right) - \log \gamma_1 = pH - pK_a^T \quad (35)$$

and we get then

$$pK_a = pK_a^T - \log \gamma_{1(T=0.5)} = pH_{T=0.5} \quad (36)$$

2. MATERIAL AND METHODS

2.1. Reagents

Acetic acid (CH_3COOH) $M=60$ g/mol (Merck > 99.5%, 1.049 g/mL); Alanine ($NH_2CH_2CH_2COOH$) $M=89.09$ g/mol (Merck, analytical grade); Chloroacetic acid ($ClCH_2COOH$) $M=94.5$ g/mol (Merck > 99.5%); Tris(hydroxymethyl)-aminomethane (TRIS) ($(HOCH_2)_3CNH_2$) $M=121.14$ g/mol (Merck > 99.5%); Sodium chloride (NaCl) $M=58.44$ g/mol (Merck, analytical grade); 1M hydrochloric acid (HCl) (Merck, analytical grade); Potassium hydroxide (KOH) 1M (Merck, analytical grade); Water for ACS analysis (Panreac).

2.2. Instruments

Analytical balance (Metler AE200) (4 decimals), pH-meter Crison GPL 21 Model (3 decimals), burette of 5 mL (Brand) (± 0.01 at 20 °C), burette of 2 mL (Brand) (± 0.01 at 20 °C).

2.3. Titrations

Potentiometric Titration of Acid with Potassium Hydroxide (0.1 M) or Base with Hydrochloric Acid (0.1 M)

Fifty mL of 0.01 M or 0.001 M acid (chloroacetic acid, acetic acid, alanine) solution (see Table 2) is pipetted into a 100 mL beaker. Then the acid solution was titrated potentiometrically with potassium hydroxide solution 0.1 M (or 0.01 M) using the glass pH electrode and a burette of 5 mL (or 2 mL). At fixed $I=0.1$ (NaCl) ionic strength, 100 mL 0.005 M of acid solutions (and 0.1 M in NaCl) were titrated with potassium hydroxide 0.1 (and 0.1 M in NaCl). TRIS 0.01 M was also titrated with 0.1 M hydrochloric acid solution at varying ionic strength.

Table 2. Evaluation of acidity constants of acidic compounds (bilogarithmic method)

Compound	V_0	C_A	C_B	I	a_1	a_0	pK_a^T	pKa
$ClCH_2COOH$	50	0.0103	0.1	var	-1.008	2.766	2.744 ± 0.006	2.600 ± 0.010
	100	0.00515	0.1	0.1	-1.010	2.623		
CH_3COOH	50	0.00098	0.01	var	-1.003	2.756	2.746 ± 0.030	4.525 ± 0.004
	100	0.005	0.1	0.1	-0.998	4.517		
$NH_2CH_2CH_2COOH$	50	0.01	0.1	var	-0.891	9.086	10.202 ± 0.003	10.007 ± 0.005
	100	0.005	0.1	0.1	-0.916	9.163		
Compound	V_0	C_B	C_A	I	a_1	a_0	pK_a^T	pKa
$(HOCH_2)_3CNH_2$	50	0.010013	0.1	var	0.982	-8.039	8.190 ± 0.005	

3. RESULTS AND DISCUSSION

The experimental results obtained are summarized in Table 2. The thermodynamic acidity constants obtained for chloroacetic and acetic acid are similar to the values compiled by Shiels and Seybold [39] (pK_a equals to 2.70 and 2.74, respectively). A good agreement is also observed between the value given by Albert and Serjeant [11] for TRIS, $pK_a=8.18$, by the value obtained by us. On the other hand a pK_a value of the order of 10.2 has been reported for β -alanine [40]. Figures 5 and 6 show the pK_a graphical bilogarithmic method for chloroacetic acid 0.001 M and alanine 0.01 M, respectively, with the residual analysis [41] included. In Table 3 are compiled together with the pK_a values obtained, the value of pH at the half titration ($T=0.5$), and both the experimental value of T when $pH=pK_a$ and the (approximate) theoretical value predicted. It can be seen that [3, 4, 42] the pH value a T ($pH=pK_a$) is < 0.5 when $pK_a \ll 7$, and $T(pH=pK_a)$ is >0.5 for $pK_a \gg 7$. That is, $pH(T=0.5) > pK_a$ in the range of acid pK_a values, and $pH(T=0.5) < pK_a$ in the alkaline pK_a range side.

Table3. Comparison values among pK_a , pH at $T=0.5$ and T at a $pH=pK_a$

Compound	C	I	pK_a^T	pK_a	$pH(T=0.5)$	T (exp.) ($pH=pK_a$)	T (theory) ($pH=pK_a$)
ClCH ₂ COOH	0.01	var	2.744		2.946	0.324	0.269
	0.005	0.1		2.600	2.975	< 0	-0.001
	0.001	var	2.746		3.500	< 0	-0.460
CH ₃ COOH	0.01	var	4.729		4.712	0.510	0.500
	0.005	0.1		4.525	4.540	0.492	0.500
NH ₂ CH ₂ CH ₂ COOH	0.01	var	10.202		10.146	0.530	0.524
	0.005	0.1		10.007	9.979	0.517	0.530
(HOCH ₂) ₃ CNH ₂	0.01	var	8.190		8.207	0.510	0.500

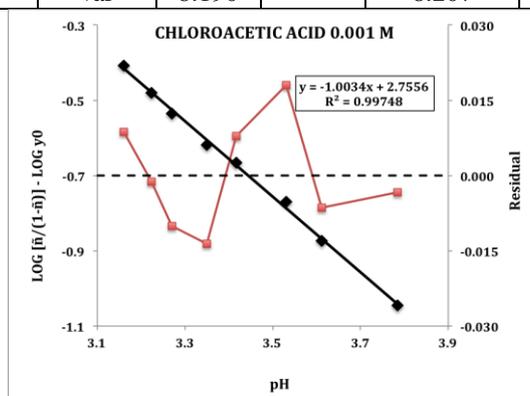


Figure5. Bilogarithmic method for the potentiometric evaluation of pK_a of chloroacetic acid

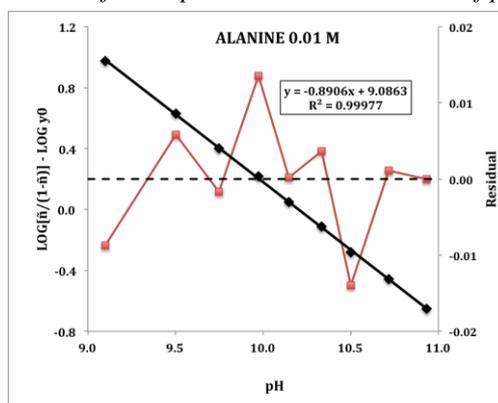


Figure6. Bilogarithmic method for the potentiometric evaluation of acidity constants of alanine

4. CONCLUSION

Therefore, the usual criterion of $pK_a = pH$ should be adopted with caution, since it is not applicable to very weak and highly diluted acids, or to medium strength and diluted acids. A look at Table 1 shows that this criterion is used with a certain frequency, having been applied to Raman, potentiometric, ion exchange, flow ratiometry, and liquid chromatographic among other measurements, although under

favourable conditions. Meija and Biseniek [18, 19] have also deal with this topic. However it is convenient to make as complete a use as possible [43] of the experimental data obtained. On this respect the use of the bilogarithmic method (Fig. 5 and 6) should be advocated.

REFERENCES

- [1] Michalowska-Kaczmarczyk A. M., Michalowski T., Asuero A. G., Inflection points on some S-shaped curves, *J. Anal. Sci. Methods Instr.* 4, 27-30 (2014).
- [2] Asuero A. G., Michalowski T., Comprehensive formulation of titration curves for complex acid-base system and its analytical implications, *Crit. Rev. Anal. Chem.* 41, 151-187 (2011).
- [3] Meites L., Goldman J. A., Theory of titration curves. Part I, The locations of inflection points on acid-base and related titration curves, *Anal. Chim. Acta* 29, 472-479 (1963).
- [4] Meites L., Goldman J. A., Theory of titration curves. Part III, The locations of points at which $pH = pK_a$ on potentiometric acid-base titration curve; end-point errors in titrations to predetermined pH values, *Anal. Chim. Acta* 30, 28-33 (1964).
- [5] Le Duigou Y., Calcul de la position du point final de la courbe de titration potentiométrique de l'acide borique, Technical Report EUR-2240.f, NSA-19-032057, European Atomic Energy Community, Gelel (Belgium). Central Nuclear Measurements Bureau, (1965).
- [6] Roller P. S., Theory of the end point in electrometric titration, *J. Am. Chem. Soc.* 50 (1), 1-8 (1928).
- [7] Roller P. S., Theory of the error of acid-base titration, *J. Am. Chem. Soc.* 54, 3485-3499 (1932).
- [8] Roller P. S., Theory of the error of acid-base titration, *J. Am. Chem. Soc.* 57, 98-99 (1935).
- [9] Stokes R. H., Equivalence point and inflexion points in acid-base titration curves, *Australian J. Chem.* 16 (5), 759-773 (1963).
- [10] Fournaise R., Petitfaux C., Limites à l'emploi des points d'inflexion comme points d'équivalence lors de l'exploitation des titrages acido-basiques. Intérêt de l'affinement multiparamétrique pour une analyse précise des données potentiométriques, *Analisis* 15 (1), 33-42 (1987).
- [11] Albert A., Serjeant E.P.J., The Determination of Ionization Constants. A Laboratory Manual, 3th ed., Chapman and Hall: New York (1984).
- [12] Asuero A.G., Buffer capacity of a polyprotic acid: first derivative of the buffer capacity and pK_a values of single and overlapping equilibria, *Crit. Rev. Anal. Chem.* 37 (4), 269-301 (2007).
- [13] Koeller S., Lescure M. H., Davies C., Desvergne J. P., Massip S., Bibal B., Hydrogen-bonding amidoindoles in the presence of anions: an X-ray structure of a receptor at the acid-base half-equivalence that binds an anion, *World Eur. J. Org. Chem.* 1, 5627-5631 (2017).
- [14] Koeller S., Lescure M. H., Davies C., Desvergne J. P., Massip S., Bibal B., Insight into the deprotonation at the half equivalence point of (thio)amido-benzimidazoles in the presence of anions, *Org. Biomol. Chem.* 15, 7263-7266 (2017).
- [15] Randall J., *Advanced Chemistry with Vernier*, Fourth Ed., Vernier, Chem A (2017). ISBN 978-1-929075-83-6.
- [16] Suwandaratne N., Hu J., Siriwardana K., Gadogbe M., Zhang D., Evaluation of thiol Raman activities and pK_a values using internally referenced Raman-based pH titration, *Anal. Chem.* 88, 3624-3631 (2016).
- [17] Balázs N., Sipos P., Limitations of pH-potentiometric titration for the determination of the degree of deacetylation of chitosan, *Carbohydr. Res.* 342, 124-130 (2007).
- [18] Meija J., Bisenieks J., Half-titration challenge, *Anal. Bioanal. Chem.* 388, 993-994 (2007).
- [19] Meija J., Bisenieks J., Solution to half-titration challenge, *Anal. Bioanal. Chem.* 389, 1301-1302 (2007).
- [20] Tanaka H., Tachibana T., Determination of acid/base dissociation constants based on a rapid detection of the half equivalence point by feedback-based flow ratiometry, *Anal. Sci.* 20, 979-981 (2004).
- [21] Tanaka H., Kiriko K., Tachibana T., Chuman H., Dasgupta P. K., Determination of acid dissociation constants based on continuous titration by feedback-based flow ratiometry, *Talanta* 64, 1169-1174 (2004).
- [22] Manderscheid M., Eichinger T., Determination of pK_a values by liquid chromatography, *J. Chromatogr. Sci.* 41, 323-326 (2003).
- [23] Tanaka H., Oda R., Tachibana T., Dasgupta P. K., Determination of dissociation constants of weak acids by feedback-based flow ratiometry, *Anal. Chim. Acta* 499, 199-204 (2003).
- [24] Carlsson K., Karlberg B., Micro-volume flow titration and screening the dissociation constants (pK_a) of weak acids, *Anal. Chim. Acta* 434, 149-156 (2001).

- [25] V. S. Soldatov, A simple method for the determination of the acidity parameters of ion exchangers, *React. Func. Pol.* 46, 55–58 (2000).
- [26] Barnum D., Predicting acid–base titration curves without calculations, *J. Chem. Educ.* 76 (7), 938–942 (1999).
- [27] Soldatov V. S., Potentiometric titration of ion exchangers, *React. Func. Pol.* 38 (6), 73–112 (1998).
- [28] Kildahl N., A simpler approach to “apparent” pK_a 's *J. Chem. Educ.* 73 (6), 598 (1996).
- [29] Cawley J. J., The determination of “apparent” pK_a 's. Part II. An experiment using very weak acids (pK_a 's > 11.4), *J. Chem. Educ.* 72 (1), 88–90 (1995).
- [30] Cawley J. J., The Determination of “Apparent” pK_a 's, An Experiment for Liberal Arts or Science Students. *J. Chem. Educ.* 70 (7), 596–598 (1993).
- [31] Fernandes Diniz J. M. B., Herrington T. M., pK_a determination of weak acids over a large pH range, *J. Chem. Eng. Data*, 38 (1), 109–111 (1993).
- [32] Stephens S. J., Joncich M. J., Determination of pK_a using the half-volume method: A laboratory experiment, *J. Chem. Educ.* 54 (11), 711 (1977).
- [33] Gage J. C., The potentiometric titration of weak acids and bases in dilute aqueous solution, XVth International Congress on Pure and Applied Chemistry, 82, 219–228 (1956).
- [34] Asuero A. G., González A. G., Some observations on fitting a straight line to data, *Microchem. J.* 40 (2), 216–225 (1989).
- [35] Sayago A., Asuero A. G., Fitting straight lines with replicate observations by linear regression: Part II. Testing for homogeneity of variances, *Crit. Rev. Anal. Chem.* 34 (3-4), 133–146 (2004).
- [36] Asuero A. G., Gonzalez A. G., de Pablos F., Gomez-Ariza J. L., Determination of the optimum working range in spectrophotometric procedures, *Talanta* 35 (7), 531–537 (1988).
- [37] Martin J., Morejon M. J. B., Asuero A. G., A bilogarithmic hyperbolic sine procedure for the simultaneous calculation of successive formation constants of two step overlapping acid-base equilibria from potentiometric measurements, *Int. J. Advanced Res. Chem. Sci.* Accepted.
- [38] Liengme B. V., *A Guide to Microsoft Excel 2013 for Scientists and Engineers*, Elsevier: Amsterdam (2015).
- [39] Shields G. C., Seybold P. G., *Computational Approaches for the Prediction of pK_a Values*, CRC Press: Boca Raton, FL (2014); p. 89.
- [40] Martin J., Ruiz D. B., Asuero A. G., Determination of the end point in potentiometric titrations: Gran and Schwartz methods, *J. Lab. Chem. Educ.* 6 (4), 77–90 (2018).
- [41] Martin J., de Adana D. D. R., Asuero A. G., Fitting Models to Data: Residual Analysis, a Primer, In *Uncertainty Quantification and Model Calibration*, J. P. Hessling (ed.). IntechOpen, Chap. 7, (2017); pp. 133–173. DOI: 10.5772/68049.
- [42] Michalowski T., Pilarski B., Asuero A. G., Dobkowska A., A new sensitive method of dissociation constants determination based on the isohydric solutions principle, *Talanta* 82, 1965–1973 (2010).
- [43] Rossotti H., *The Study of Ionic Equilibria, an Introduction*, Longman: London (1978).

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