

Panta Rei Function and Light Diversity (Exercise at Seventy-Two Decimal Places)

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In this paper one investigates the meaning of the constant c in the $E = mc^2$ equivalence and of it dependent panta-rei-function $m^2 v^2 = e^{\frac{m_0^2 c^2 + m^2 (v^2 - c^2)}{k}}$ as well as extends the validity of the model to the speed beyond c . The maximal speed of the infinite self-mass c_x equals the concerned constant c . On the other hand the maximal speed of the zero self-mass c_0 equals the maximal possible speed of the real self-masses in space v_{max} . The difference $c_0 - c_x$ is expected to be tiny: on the 72th decimal or more. The extended model also provides imaginary self-masses of photons which could explain the diversity in the speed of light $c_{light} = c \sqrt{1 + \frac{k}{m_{photon}^2 c^2}}$ and the beam divergence being proportional to the wavelength λ .

Keywords: *Panta rei function, energy-mass equivalence, self-mass, mass equivalent, dynamic constant, base of natural logarithm, speed of light, gamma rays, beam divergence, Heracleitean world*

1. THEORETICAL BACKGROUND

Mass equivalent m and speed v (or relative speed $a = \frac{v}{c}$) of the mass body with the self-mass m_0 are in the panta rei function [1] related as:

$$m^2 v^2 = e^{\frac{m_0^2 c^2 + m^2 (v^2 - c^2)}{k}} \quad \text{or} \quad m^2 c^2 a^2 = e^{\frac{m_0^2 c^2 + m^2 c^2 (a^2 - 1)}{k}}. \quad (1)$$

Two constants determine the relation between the mass equivalent m and speed v (or relative speed a). The dynamic constant k mirrors the flowing nature of physical bodies and constant c reflects the energy-mass equivalence $E = mc^2$. At the zero dynamic constant k the panta rei function (1) (except for $v = 0$) transforms into the known relation of the classic relativistic dynamics in the non-Heracleitean world where c means the speed of light which in the same time plays the role of the maximal possible speed of mass bodies in space:

$$m_0^2 c^2 + m^2 (v^2 - c^2) = 0 \quad \text{or} \quad m_0^2 c^2 + m^2 c^2 (a^2 - 1) = 0. \quad (2)$$

The question is raised if the equality between the energy-mass equivalence constant, denoted c , and the speed of light as the maximal possible speed in space, also denoted c , holds true in the Heracleitean world determined with the dynamic constant $k \geq 0$. The matter of fact, our concern in this paper is to find out the difference between both values, if at all there is any.

To facilitate the mathematical manipulation the panta rei function (1) is preferred to be written in the substituted form. For the dependant variable $y = m^2 c^2$ and independent variable $x = a^2$ we have:

$$yx = e^{\frac{m_0^2 c^2 + y(x-1)}{k}}. \quad (3)$$

With the help of derivation of the panta rei function the maximal value at the infinite tangent of that function can be found.

2. THE DERIVATION OF THE PANTA REI FUNCTION

Making \ln of both sides of the equation (3) gives:

$$\ln y + \ln x = \frac{m_0^2 c^2 + yx - y}{k}. \quad (4)$$

The derivation $\frac{dy}{dx}$ gives:

$$\frac{y'}{y} + \frac{1}{x} = y'x/k + y/k - y'/k. \quad (5)$$

Rearranging gives:

$$\begin{aligned} \frac{y'}{y} - \frac{y'}{k}(x-1) &= \frac{y}{k} - \frac{1}{x}, \\ y' \left(\frac{1}{y} - \frac{x-1}{k} \right) &= \frac{y}{k} - \frac{1}{x}, \\ y' &= \frac{\frac{y}{k} - \frac{1}{x}}{\frac{1}{y} - \frac{x-1}{k}}. \end{aligned} \quad (6)$$

3. THE INFINITE-TANGENT OF THE PANTA REI FUNCTION

The infinite tangent is found when the nominator of the fraction(6)is zero.

$$y' = \infty \rightarrow \frac{1}{y} - \frac{x-1}{k} = 0 \rightarrow y(x-1) = k. \quad (7)$$

The result is valid since at the same time the numerator is positive independently of the value of the dynamic constant k :

$$\frac{y}{k} - \frac{1}{x} = \frac{1}{x-1} - \frac{1}{x} > 0 \text{ for } 0 \leq k \leq 1. \quad (8)$$

The values of y and x are found with the help of relations (7) and (3) as follows:

$$\begin{aligned} yx &= y + k \text{ and } x = 1 + \frac{k}{y}, \\ yx &= e^{\frac{m_0^2 c^2 + y(x-1)}{k}}, \\ y + k &= e^{\frac{m_0^2 c^2 + k}{k}}, \\ y &= e^{\frac{m_0^2 c^2}{k} + 1} - k \text{ and } x = 1 + \frac{k}{e^{\frac{m_0^2 c^2}{k} + 1} - k}. \end{aligned} \quad (9)$$

4. THE MAXIMAL MASS EQUIVALENT

Expressing the relation (7)with the help of the origin variables the maximalvalue at the infinite-tangent of the panta rei function is given:

$$m^2 c^2 (a^2 - 1) = m^2 (v^2 - c^2) = k. \quad (10)$$

Expressing the relations (9) with the help of origin variables the maximal relative speed a_{max} and maximal mass equivalent m_{max} are given as:

$$a_{max}^2 = \frac{v_{max}^2}{c^2} = 1 + \frac{1}{\frac{e^{\frac{m_0^2 c^2}{k} + 1}}{k} - 1}. \quad (11)$$

$$m_{max}^2 c^2 = e^{\frac{m_0^2 c^2}{k} + 1} - k. \quad (12)$$

Combining equations (11),(12) the maximal momentum $p_{max} = m_{max}v_{max}$ is given as:

$$p_{max}^2 = m_{max}^2 v_{max}^2 = e^{\frac{m_0^2 c^2}{k} + 1}. \quad (13)$$

The maximal value of speed v_{max} (11), mass equivalent m_{max} (12) as well as momentum $p_{max} = m_{max}v_{max}$ (13) is not unique but is at the given dynamic constant k ofthe self-mass m_0 dependent.

5. THE WINDOW OF MAXIMAL SPEEDS

The window of maximal speeds of mass bodies is given with the help of the relation(11) which can be written in the explicit form as:

$$v_{max} = c \sqrt{1 + \frac{1}{\frac{e^{\frac{m_0^2 c^2}{k} + 1}}{k} - 1}}. \quad (14)$$

The lowest maximal speed v_{max}^{min} is achieved at the infinite self-mass of the mass body $m_0 = \infty$:

$$v_{max}^{min} = v_{max}(m_0 = \infty) = c_\infty = c \sqrt{1 + \frac{1}{\infty}} = c. \quad (15)$$

On the other hand the highest maximal speed v_{max}^{max} is achieved at the zero self-mass of the mass body $m_0 = 0$:

$$v_{max}^{max} = v_{max}(m_0 = 0) = c_0 = c \sqrt{1 + \frac{1}{\frac{e}{k} - 1}}. \quad (16)$$

The window of maximal speeds of mass bodies v_{max} extends from the maximal speed of the infinite self-mass of the mass body c_∞ to maximal speed of the zero self-mass of the mass body c_0 :

$$c_\infty < v_{max} < c_0 = c_\infty \sqrt{\left(1 - \frac{k}{e}\right)^{-1}}. \quad (17)$$

The window (17) is open in the Heraclitean world determined with the positive dynamic constant $k > 0$. The lower limit of the above window, denoted c_∞ , represents the energy-mass equivalence constant c . On the other hand the upper limit, denoted c_0 , represents the maximal possible speed of mass bodies in space v_{max}^{max} which could equal the speed of light. If so – to escape the confusion - the speed of light should be denoted c_{light} instead of c .

The window of maximal speeds of mass bodies is detained in the downsizing Heraclitean world determined by the zero dynamic constant $k = 0$ since there the maximal speed v_{max} is independent of the self-mass m_0 (14):

$$c_\infty = v_{max} = c_0. \quad (18)$$

The concerned window is also detained in the non-Heraclitean world where the dynamic constant is absent(2) since there no real self-mass can exceed the maximal speed $v_{max} = c$ (2):

$$m = \frac{m_0}{\sqrt{\left(1 - \frac{v^2}{c^2}\right)}} \text{ for } v \leq c. \quad (19)$$

At the detained window of maximal speeds of mass bodies the speed of light could equal the energy-mass equivalence constant c as well as represent the maximal possible speed of mass bodies in space v_{max}^{max} and could be denoted on c as before.

Let us resume. The maximal possible value of speed v_{max}^{max} equals the constant c only exceptionally. First, in the downsizing Heraclitean world where k is zero(11). Secondly, in the non-Heraclitean world where k is absent(2). In the Heraclitean world with $k > 0$ the maximal speed of mass body with the finite self-mass m_0 always exceeds the constant c . The same is true with the speed of light c_{light} , if it should subordinate the greatest possible speed in space.

6. THE SELF-MASS AND THE SPEED OF LIGHT

Assuming the Panta rei function is valid also for the electro-magnetic wave energy particles (photons) the equation (12) bringing the relation between the maximal mass equivalent m_{max} and the self-mass m_0 can be applied also for them. Let it be written in the inverse form:

$$m_0 = \frac{\sqrt{k(\ln(m_{max}^2 c^2 + k) - 1)}}{c}. \quad (20)$$

The next question is raised. If the speed of light should equal the greatest possible speed in space, the self-mass of the photon m_0 may not be non-zero since according to the window of maximal speeds the speed of non-zero self-masses is lower(11). To resolve the problem let us analyse the equation (20) first.

The self-mass m_0 of the photon is real only when the expression under the square root(20) is positive or zero. It can be examined that it happens for the next values of the maximal mass equivalent of photon:

$$m_{max} \geq \frac{\sqrt{e-k}}{c} \approx \frac{\sqrt{e}}{c} \text{ then } m_0 \in \mathbb{R}^+. \tag{21}$$

Real maximal mass equivalent m_{max} and real self-mass m_0 are in direct proportion to each other(20). Greater real self-mass m_0 corresponds to the greater real maximal mass equivalent m_{max} and vice versa.

On the contrary, the self-mass m_0 of the photon is imaginary when the expression under the square root(20) is negative. It happens for the next values of the maximal mass equivalent of photon:

$$m_{max} \leq \frac{\sqrt{e-k}}{c} \approx \frac{\sqrt{e}}{c} \text{ then } m_0 \in \mathbb{R}^+ x i. \tag{22}$$

Real maximal mass equivalent m_{max} and imaginary self-mass m_0 are inversely proportional to each other(20)(12). Greater imaginary self-mass m_0 corresponds to the smaller real maximal mass equivalent m_{max} and vice versa. This can be easily seen if the formula(12) is rewritten for the imaginary self-masses $m_{0,i} = im_0$ since the exponent changes the sign:

$$m_{max}^2 c^2 = e^{-\frac{m_{0,i}^2 c^2}{k} + 1} - k. \tag{23}$$

Even the heaviest photons of gamma-rays possess mass equivalents of the magnitude far less than $\frac{\sqrt{e}}{c}$ so we can assume that self-masses of the light are imaginary. But their speed(11) is real:

$$v_{max} = c \sqrt{1 + \frac{1}{\frac{e^{-\frac{m_{0,i}^2 c^2}{k} + 1}}{k} - 1}}. \tag{24}$$

And their momentum is real, too:

$$p_{max}^2 = m_{max}^2 v_{max}^2 = e^{-\frac{m_{0,i}^2 c^2}{k} + 1}. \tag{25}$$

7. THE TYPE OF THE MASS BODY PARTICLE

Some extreme characteristics of mass bodies regarding the type of mass body particle are collected in the Table1.

Table1. Some characteristics of the real, zero and imaginary self-mass particles

Type of Particle	Real Particle	Zero Particle	Imaginary Particle
Self-mass $m_0(kg)$	$\infty > m_0 > 0$	0	$0 < m_0 < \frac{\sqrt{k(lnk-1)}}{c}$
Maximal mass equivalent $m_{max}(kg)$	$\infty > m_{max} > \frac{\sqrt{e-k}}{c}$	$m_{max} = \frac{\sqrt{e-k}}{c}$	$\frac{\sqrt{e-k}}{c} > m_{max} > 0$
Maximal speed $v_{max}(\frac{m}{s})$	$c < v_{max} < c \sqrt{\left(1 - \frac{k}{e}\right)^{-1}}$	$v_{max} = c \sqrt{\left(1 - \frac{k}{e}\right)^{-1}}$	$c \sqrt{\left(1 - \frac{k}{e}\right)^{-1}} < v_{max} < \infty$
Maximal momentum $\left(\frac{kg^2 m^2}{s^2}\right)$	$\infty > p_{max} > \sqrt{e}$	$p_{max} = \sqrt{e}$	$\sqrt{e} > p_{max} > \sqrt{k}$
Maximal energy $E_{max}(J)$	$\infty > E_{max} > c\sqrt{e-k}$	$E_{max} = c\sqrt{e-k}$	$c\sqrt{e-k} > E_{max} > 0$

$k = \text{dynamic constant, } e = \text{base of natural logarithm, } c = \text{energy - mass equivalence constant}$

In the above table is evident, for instance, that the maximal speed of the imaginary particle (light) $v_{max} = c_{light}$ spreads regarding the value of its self-mass m_0 from the maximal speed of the zero self-mass $c_0 = c\sqrt{\left(1 - \frac{k}{e}\right)^{-1}}$ to the infinite speed $c_{light} = \infty$:

$$c_{light} \geq c_0 = c\sqrt{\left(1 - \frac{k}{e}\right)^{-1}}. \tag{26}$$

The slowest speed of light $v_{max} = c_0$ (26) belonging to the self-mass $m_0 = 0$ and mass equivalent $m_{max} = \frac{\sqrt{e-k}}{c}$ is the upper limit of the speed of real mass bodies in the Heracleitean world.

8. THE FASTEST LIGHT AND THE GROUND CIRCUMSTANCES

Further it is evident from the Table 1 that the fastest speed of light $v_{max} = \infty$ belonging to the self-mass $m_0 = \frac{\sqrt{k(tk-1)}}{c}$ and mass equivalent $m_{max} = 0$ can be considered to bring instantly the maximal momentum $p_{max} = \sqrt{k}$ as a ground momentum p_{ground} [1] to every bit of the Heracleitean world. Since recalling the characteristics of the dynamic constant k [1] as a product of extreme momenta p_{min} and p_{max} holds:

$$k = p_{min} \times p_{max} = \sqrt{k} \times \sqrt{k}. \tag{27a}$$

So:

$$p_{min} = p_{max} = p_{ground}. \tag{27b}$$

It looks like the fastest light maintains the ground circumstances [1] for which no outer impulse or work is needed. Further, taking the relation (27b) as the rotational momentum p_{min} being equal the translational momentum p_{max} one can explain the ground momentum in no direction is preferable.

9. THE PHOTON MASS EQUIVALENT AND THE SPEED OF LIGHT

Combining the equations (12), (14) the relation between the maximal speed $v_{max} = c_{light}$ and the maximal mass equivalent $m_{max} = m_{photon}$ is given:

$$c_{light} = c\sqrt{1 + \frac{k}{m_{photon}^2 c^2}}. \tag{28}$$

From the above equation (28) follows that heavier photons (with more mass equivalent) should be slower than lighter photons (with less mass equivalent). The difference is tiny according to the expected extremely low dynamic constant k [2]. However, it could explain why astronomers studying radiation coming from a distant galaxy found that the high energy gamma rays arrived a few minutes after the lower-energy photons, even though they were emitted at the same time [3].

10. THE DISTRACTIVE FORCES BETWEEN PHOTONS

Gravitational law rules the mass bodies possessing the self-mass m_0 :

$$F = G \frac{(m_0)_1 \times (m_0)_2}{r^2}. \tag{29}$$

Inserting some imaginary self-masses of photons in the above equation we see that the gravitational force between photons becomes distractive ($i \times i = -1$). This feature could explain why the beam of photons is cone-shaped [4]. Further the fact that lighter photons are more imaginary and consequently more distractive (22) can explain the divergence of the light beam. Indeed, the angular spread of the beam is proportional to the wavelength $\lambda = \frac{h}{mc}$ [4] which is in direct proportion to the imaginaries of photons (23).

11. FROM THE ENERGY-MASS EQUIVALENCE CONSTANT c_0 TO THE DIVERSE SPEED OF LIGHT c_{light}

The equations(17), (26) can be rewritten in the explicit form for the energy-mass equivalence constant c as follows:

$$c = c_{\infty} = \sqrt{1 - \frac{k}{e}} c_0 \leq c_0 \leq c_{light}. \quad (30a)$$

c = energy – mass equivalence constant

c_{∞} = the maximal speed of the infinite self – mass

c_0 = the maximal speed of the zero self – mass as well as the minimal speed of light

k = dynamic constant

e = base of natural logarithm

As already mentioned the dynamic constant k is expected to be extremely small yielding $\frac{k}{e} \leq 2 \times 10^{-72} \text{ kg}^2 \text{ m}^2 \text{ s}^{-2}$ [2], (34) so according to the equation (30a) the difference between the concerned values is hardly detectable:

$$c = c_{\infty} \leq \sqrt{1 - 2 \times 10^{-72}} c_0 \leq (1 - 10^{-72}) c_0. \quad (30b)$$

All values – c, c_{∞}, c_0 – of course, equal the official speed of light $c_{light}^{official} = 2.99792458 \times 10^8 \frac{\text{m}}{\text{s}}$ [5] since they differ at most on the 72th – decimal. But in the Heracleitean world of the non-zero dynamic constant k lighter photons can significantly exceed this value all the way to the infinite one(28).

12. THE WAVELENGTH AND FREQUENCY OF PHOTONS

Applying Planck relation $E = \frac{hc_{light}}{\lambda}$, equation (28) and the energy-mass equivalence $E = m_{photon}c^2$ the relation between the mass equivalent of photon m_{photon} and its wavelength λ is given:

$$m_{photon}c^2 = \frac{hc_{light}}{\lambda} = \frac{hc}{\lambda} \sqrt{1 + \frac{k}{m_{photon}^2c^2}},$$

$$\lambda = \frac{h}{m_{photon}c} \sqrt{1 + \frac{k}{m_{photon}^2c^2}}. \quad (31)$$

The mass equivalent of photon m_{photon} and its wavelength λ are in inverse proportion independently of the value of the dynamic constant k . For instance, the wavelength λ of the zero mass equivalent of photon $m_{photon} = 0$ is infinite. This means that the fastest light brings the ground momentum $p_{ground} = \sqrt{k}$ (27b) from infinity to everywhere.

Applying the relation $c_{light} = \lambda\nu$ the relation between the mass equivalent of photon m_{photon} and its frequency ν is given:

$$\nu = \frac{c_{light}}{\lambda} = \frac{m_{photon}c^2}{h}. \quad (32)$$

The mass equivalent of photon m_{photon} and its frequency ν are in direct proportion independently of the value of the dynamic constant k . For instance, the frequency ν of the zero mass equivalent of photon $m_{photon} = 0$ is zero. This means that the fastest light brings the ground momentum $p_{ground} = \sqrt{k}$ (27b) from infinity all the time.

13. CONCLUSION REMARKS

In the previous presentation of the Panta rei force model[1] the speed of light being ad hoc the upper limit of the domain of the panta rei function $v_{max} = c$ determines the upper limit of its range at $m_{max} = \frac{1}{c} \sqrt{e^{\frac{m_0^2 c^2}{k}}}$. On the contrary, in the present article the upper limit of both intervals is determined by the panta rei function itself. For real self-masses the upper limit of range

$$m_{max} = \frac{1}{c} \sqrt{e^{\frac{m_0^2 c^2}{k} + 1} - k} \text{ is achieved at the upper limit of the domain } v_{max} = c \sqrt{1 + \frac{k}{e^{\frac{m_0^2 c^2}{k} + 1} - k}}.$$

The domain beyond this limit is reserved for imaginary self-masses (photons of light) characterised by lower mass equivalents than $\frac{\sqrt{e-k}}{c}$ becoming zero at the infinite speed. The present interpretation of the Panta rei force model takes precedence over the previous one since it can explain some (new) characteristics of light. Under the assumption and in hope, of course, we have been looking for the needle in the right haystack lately.

14. THE ADDENDUM

The new upper limit of the domain of the panta rei function leads to the prediction of the \sqrt{e} -times smaller value of the size of the point s_{point} as previously predicted[1]:

$$s_{point} = \frac{h}{\sqrt{e}}. \quad (33)$$

The new predicted size of the points s_{point} (33) leads to the prediction of the \sqrt{e} -times smaller value of the dynamic constant k as previously predicted[2]:

$$k = \frac{m_e^3 \alpha^3 c^3}{\sqrt{e}} kg^{-1} m^2 s^{-2} = \frac{7.9145 \times 10^{-72}}{\sqrt{e}} kg^2 m^2 s^{-2} = 4.8004 \times 10^{-72} kg^2 m^2 s^{-2}. \quad (34)$$

The new predicted value of the dynamic constant k (34) leads to the prediction of the e -times greater value of the size of the entire universe $s_{universe}$ as previously predicted[2]:

$$s_{universe} = \frac{h}{k} \sqrt{e} = 2.276 \times 10^{38} m. \quad (35)$$

Respecting the present theory the sub-point and super-universe sizes are reserved for the imaginary self-mass particles, i.e. photons of light.

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Dedication

This fragment is dedicated to pharmacy as a profession and art.

REFERENCES

- [1] Špringer J. *Panta rei as $F = dp/dt + d(k/p)/dt$ and Possible Geometric Consequences.* *International Journal of Advanced Research in Chemical Science (IJARCS)*, Volume 1, Issue 6, August 2014, 36-46.
- [2] Špringer J. *From Dynamic Constant to Inner Energy and Size of Universe.* *International Journal of Advanced Research in Chemical Science (IJARCS)*, Volume 1, Issue 10, December 2014, 9-12.
- [3] Gamma Ray Delay May be Sign of “New Physics”. <http://news.ucdavis.edu/search/news/detail.lasso?id=8364>, Retrieved February 2015
- [4] Svelto O. *Principles of Lasers. 5th Edition.* Springer, 2009, 153-155.
- [5] CODATA, Values of the Fundamental Constants. http://physics.nist.gov/cgi-bin/cuu/Value?c/search_for=universal_in!. Retrieved February 2015